### Introduction

Biological liquid-liquid phase-separation plays an important role in the formation of cellular microstructures and protein organization. Experiments have shown that proteins (SynGAP and PSD-95) exhibit liquid-liquid phase transitions in neuronal structures and may influence the formation of postsynaptic densities (PSD) [1]:

- SynGAP and PSD-95 bind with high affinity.
- SynGAP trimer form a 3:2 complex with two PSD-95.
- 3:2 complex undergoes phase transitions.



Figure 1: Phase separation of SynGAP and PSD-95 [1].

### Objectives

- Model drift-diffusion at particle and ensemble scales that incorporates geometry.
- Include intermolecular and external forces on proteins.
- Phase separation model coupled to proteins.



### Drift-Diffusion Markov Chain

### **Transition Probabilities:**



Figure 2: Simplified Markov Chain

### **Ginzburg-Landau Field**

### **Potential Energy:**

Nearest Neighbors Similar

$$V[q] = \alpha_1 \sum_{i} \sum_{j \neq i} W_{ij} (q_i - q_j)^2$$
Phase Collapses to ±1
$$+ \alpha_2 \sum (1 - q_i^2)^2 .$$
(2)



Figure 3: Ginzburg-Landau Field. Click here for animation.

Figure 5: Number of protein clusters on different surfaces, averaged over  $\sim 50$  simulations.

# **Computational Models of Protein Phase Separation on Curved Surfaces**

### Results



Figure 4: SynGAP/PSD95 clustering simulations on planar, cylindrical, and spherical surfaces. Click here for animations.



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### Conclusion

• Developed model incorporating geometry and protein dynamics at continuum and particle level dynamics.

• Analyzed the role of geometry in clustering of proteins.

• Applied to protein phase separation of SynGAP and PSD-95 clustering in neuronal dendritic spines.

### References

[1] M. Zeng et al. Phase transition in postsynaptic densities underlies formation of synaptic complexes and synaptic plasticity. *Cell*, 166:1163–1175, 2016.

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